## **Real Numbers**

#### **Euclid's Division Lemma**

- An algorithm is a series of well defined steps which gives a procedure for solving a type of problem.
- A lemma is a proven statement used for proving another statement.
- Euclid's division algorithm is a technique to compute the Highest Common Factor (HCF) of two given positive integers.
- To obtain the HCF of two positive integers, say c and d, with c > d, follow the steps below: Step 1: Apply Euclid's division lemma, to c and d. So, we find whole numbers, q and r such
  - Step 2: If r = 0, d is the HCF of c and d. If  $r \neq 0$ , apply the division lemma to d and r.
  - Step 3: Continue the process till the remainder is zero. The divisor at this stage will be the required HCF.

## The Fundamental Theorem of Arithmetic

• Every composite number can be expressed (factorized) as a product of primes, and this factorization is unique, apart from the order in which the prime factors occur.

#### **Rational and Irrational Numbers**

that c = dq + r,  $0 \le r < d$ .

- A number 's' is called rational if it can be written in the form p, q
  Where p and q are integers and q ≠ 0.
- A number 's' is called irrational if it cannot be written in the form p, q Where p and q are integers and  $q \neq 0$ .

# Irrationality of Square Roots of 2, 3 and 5

- Let p be a prime number. If p divides a<sup>2</sup>, then p divides a, where a is a positive integer.
- $\sqrt{2}$ ,  $\sqrt{3}$ ,  $\sqrt{5}$  are irrational

## **Decimal Expansions of Rational Numbers**

- Let x be a rational number whose decimal expansion terminates. Then we can express x in the form pq, where p and q are coprime, and the prime factorization of q is of the form 2<sup>n</sup>5<sup>m</sup>, where n, m are non-negative integers.
- Let x = pq be a rational number, such that the prime factorization of q is of the form  $2^n5^m$ , where n, m are non-negative integers. Then x has a decimal expansion which terminates.
- Let x = pq be a rational number, such that the prime factorization of q is not of the form  $2^n 5^m$ , where n, m are non-negative integers. Then x has a decimal expansion which is non-terminating repeating (recurring).